

GRAPHICAL METHOD FOR DETERMINING ATMOSPHERIC PRESSURE FROM ROCKETSONDE OBSERVATIONS

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ABSTRACT

A graphical method of determining pressure from rocketsonde temperature-measurements is presented, and information for the construction and use of such a graph is given. This graphical method is shown to be simple and rapid. Comparison with results from computer processing of the same temperature data yields pressure differences of only 0.5 percent in 72 percent of the cases, and 1 percent in 90 percent of the cases.

1. INTRODUCTION

The rocket-boasted meteorological instrument package represents a valuable tool for measuring atmospheric parameters in the region between balloon and satellite levels. Before the Meteorological Rocket Network (MRN) was established in 1959 the acquisition and processing of rocketsonde data were carried out by many groups with similar objectives but without complete knowledge of each other's activities. With the founding of the MRN, the U.S. Army Electronics Research and Development Activity (ERDA)—formerly the U.S. Army Signal Missile Support Agency—of White Sands Missile Range, N. Mex., voluntarily undertook the task of processing and publishing data acquired by the various groups. Presently the responsibility of publishing the monthly digest lies with the Environmental Science Services Administration's (ESSA) Environmental Data Service, National Records Center, Asheville, N.C. This effort has been an important aspect of these groups' participation in the MRN, and allowed:

- (a) all data to be archived, and available in a monthly digest [1] for use by the participants, and
- (b) a single computer program to be utilized for processing all data received for inclusion in the digest [2].

The uniform reduction of the rocket data was possible through the cooperation of the participating rocket ranges in sending their data to ERDA at White Sands. These data records contained temperature, tabulated rawinsonde, and radar plotboard recordings. The radar plotboard records were considered to be a common denominator to all ranges and were used for determining altitude and wind data. When some stations lost their radar plotting board facilities and others developed specialized techniques unique to their requirements, it was decided that each contributor should be responsible for the accurate reduction of its own data. The finished product

is still forwarded to ERDA at White Sands for processing and subsequent publication by ESSA in the monthly digest. The processing will also be undertaken by ESSA with the July 1966 data.

In order to satisfy the needs of the real-time user of rocketsonde data, a rapid and efficient method of data reduction is needed. If computers are not readily available, an alternate approach must be used. The graphical method described here for determining pressure from observed temperature is one answer to the problem. This technique consists of a straightforward solution of the hydrostatic equation and equation of state. Construction and utilization of the graph are relatively uncomplicated and rapid.

2. PRESSURE COMPUTATION

In order to determine atmospheric pressure from a given temperature-height profile the hydrostatic equation

$$dp = -\rho g dz \quad (1)$$

and equation of state

$$p = \rho R T \quad (2)$$

are combined to obtain the relation

$$dp/p = -(g/RT) dz. \quad (3)$$

Integration of (3) from the pressure p_0 at height z_0 to pressure p_1 at height z_1 yields

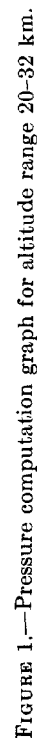
$$\ln (p_1/p_0) = -(1/R) \int_{z_0}^{z_1} (g/T) dz. \quad (4)$$

This relationship may be replaced by the excellent approximation

$$\ln (p_1/p_0) \cong -g' \Delta z / RT' \quad (5)$$

or

$$p_1/p_0 \cong \exp (-g' \Delta z / RT') \quad (6)$$



where R is the gas constant for dry air, g' is the acceleration due to gravity at the mean height of the stratum Δz and at 45° Lat., and T' is the mean (absolute) temperature of the stratum. The pressure profile is generated by employing the last-obtained p_1 as the initial pressure p_0 in each successive stratum. This procedure is employed both in the graphical method to be described, and in the computer reduction of rocketsonde temperature data [3].

3. CONSTRUCTING THE DIAGRAM

The lower portion of the graph developed for the determination of pressure is shown in figure 1. Three parameters determine the graph: temperature, height, and the pressure ratio p_1/p_0 . The scales of 1 km. and 10° C. per in. for the ordinate and abscissa, respectively, were selected to give both adequate resolution for plotting and reasonable overall diagram size. However, although a temperature range of -80° C. to 40° C. can conveniently be placed on one graph, an altitude range of 20 km. to 62 km. (the interval normally obtained in a rocket sounding) requires a representation four times larger. Therefore a complete set of diagrams includes three graphs in addition to that shown in figure 1. Furthermore, it is desirable to allow for a 1- to 2-km. overlap between successive charts.

Values of the pressure ratio (p_1/p_0) were computed for 1-km. layers. The extreme values of the temperature scale (-80° C. to 40° C.) yield a range for p_1/p_0 of approximately 0.840 to 0.899. The location of the tick marks, which represent p_1/p_0 at intervals of 0.001, is then obtained as a function of temperature from the relation

$$T' = -g' \Delta z / [R \ln (p_1/p_0)] \quad (7)$$

which is simply a rearrangement of equation (5).

4. USING THE DIAGRAM

The rocketsonde temperature and height parameters required for graphical determination of the pressure are generally obtained from direct temperature sensor measurements and radar evaluation, respectively. As temperatures and corresponding times are selected from a telemetry record, it is convenient to enter values on a form such as the Thermodynamic Data Tabulation Form (fig. 2). The altitude versus time record obtained from radar is correlated with the temperature-time information to give temperature as a function of height, which is then plotted on the pressure-computation diagram (fig. 1).

The initial pressure value required for developing a pressure-altitude profile is extracted from the rawinsonde observation (fig. 3) closest in time to the rocketsonde launching. It should be noted that in order for the procedure to be valid, reasonable agreement must exist between rocketsonde and rawinsonde temperatures at the base level.

In the case to be discussed, rocketsonde temperatures are available down to 20 km. and agree quite well with the rawinsonde temperatures. Therefore, rawinsonde data

MET ROCKET THERMODYNAMIC DATA TABULATION FORM

STATION WALLOPS ISLAND, VA. Model No. 11-2257 Motor Type ARCAS

Lat. 37° 51' N Long. 75° 29' W Payload ARGASONDE 1-A Sensor Type 10 mil bead

Year 1966 Month Jan. Day 20 Zero Time 1043 Ground Tracking Equip. GND-1B & FPS-16

75th Mer. 1966 GCT 1966 Jan. 20 1543

Calibration Check # 78.3 Ref. Ord. 89.9 Freq. Ratio 0.871 % Not required for differences less than $\pm 1.0^\circ$ C.

Calibration Temp. 24.4 °C Ambient Temp. 24.6 °C Corr. 0 °C

Time MIN. & Sec.	REF. ORD.	TEMP. ORD.	FREQ. RATIO THERM RESIS.	TEMP. °C	CORR. # TEMP. °C	PRESS. # mb.	DENSITY # gm	S O S -1 -2	ALTITUDE (geometric)		H km
									feet x 10 ²	meters x 10 ¹	
1 2139	90.4	57.3	0.634	-7.2					1534	4676	
2 2149	90.5	57.3	0.633	-7.2					1510	4602	
3 2158	90.5	56.0	0.618	-8.7					1494	4554	
4 3136	90.6	59.4	0.657	-5.0					1430	4359	
5 3141	90.6	57.3	0.632	-7.2					1420	4328	
6 3157	90.6	58.7	0.648	-5.5					1400	4267	
7 4108	90.7	56.7	0.625	-8.0					1383	4215	
8 4130	90.9	59.1	0.650	-5.3					1350	4115	
9 4154	91.0	55.0	0.604	-10.0					1322	4029	
10 5101	91.0	50.7	0.557	-14.7					1312	3999	
11 5128	91.0	53.4	0.587	-11.7					1280	3901	
12 5139	91.0	51.4	0.565	-13.8					1269	3868	
13 5149	91.0	46.7	0.513	-18.8					1259	3837	
14 6149	91.1	57.3	0.629	-7.7					1198	3652	
15 6157	91.1	56.4	0.619	-8.5					1192	3633	
16 7117	91.1	43.3	0.475	-22.3					1172	3572	
17 7124	91.1	43.0	0.472	-22.6					1164	3548	
18 7128	91.1	40.7	0.447	-25.0					1162	3542	
19 7158	91.1	33.4	0.367	-32.5					1138	3469	
20 8118	91.1	32.3	0.355	-33.7					1122	3420	
21 8140	91.1	32.5	0.357	-33.8					1104	3365	
22 8143	91.1	30.8	0.338	-35.6					1100	3353	
23 8152	91.1	32.2	0.353	-34.1					1095	3338	
24 11142	91.2	20.3	0.223	-60.9					982	2993	
25 12156	91.2	20.1	0.220	-61.4					947	2886	
26 15124	20.7	15.4	0.170	-60.0					876	2670	
27 17126	20.3	18.1	0.200	-54.2					847	2582	
28 19103	20.0	14.4	0.160	-62.6					806	2457	
29 26141	88.2	14.8	0.168	-60.9					697	2124	
30 30117	87.5	14.0	0.160	-62.7					656	2000	

REMARKS:

If applicable * Derived Values

FIGURE 2.—Sample thermodynamic data tabulation form.

RAWINSONDE OBSERVATIONS FOR METEOROLOGICAL ROCKETS
WEATHER BUREAU SUPPORT FACILITY
WALLOPS ISLAND, VIRGINIA

Prepared By: M. Powell Lat: 37° 51' N Long: 75° 29' W

Model No. 11-2527

R/S No. 79

Year 1966 Month Jan. Day 20 Release 0615 At Top 0752 Distance to Rocket Launch

GCT 1966 Jan. 20 1115 1252 Miles 0.48 Dir. 205°

Pressure Tenths Mb.	Height		Deg. S/- 180	Spd. kts	Wind		R. H. %	Tem. °C
	Geopot.	Geometric			N-S	E-W		
1020.6	0003	0000	330	18	-14	3	69	-1.7
1000.0	165	170	332	16	-7	1	73	-3.0
850.0	1137	1140	005	20	-10	-1	80	-7.7
700.0	2924	2920	353	26	-13	2	10	-16.0
500.0	5371	5380	031	39	-18	-11	32	-32.7
400.0	6921	6930	325	36	-15	11	26	-37.5
300.0	8878	8890	299	62	-15	28		-41.2
250.0	10095	10120	289	58	-9	29		-46.0
200.0	11585	11610	276	64	-3	33		-50.5
150.0	13476	13510	278	66	-4	31		-53.0
100.0	16036	16080	279	59	-5	30		-63.2
81.0	17350	17400	284	58	-7	29		-61.7
72.0	18090	18140	286	54	-7	27		-66.0
70.0	18230	18280	287	52	-8	26		-65.3
65.0	18690	18750	289	39	-6	19		-63.2
50.0	20293	20360	281	35	-3	18		-63.0
31.0	23230	23320	272	35	-1	18		-62.7
30.0	23436	23530	272	35	-1	18		-62.2
20.0	25960	26070	273	17	-1	21		-58.2
14.5	28040	28160	277	54	-3	28		-55.0
10.0	30406	30560	268	80	1	17		-47.0
7.9	31994	32150						-41.8

FIGURE 3.—Sample tabulation of data from rawinsonde observation in support of meteorological rocket firing.

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